

Name: _____

Date: _____

Complete the following table using each polynomial function:

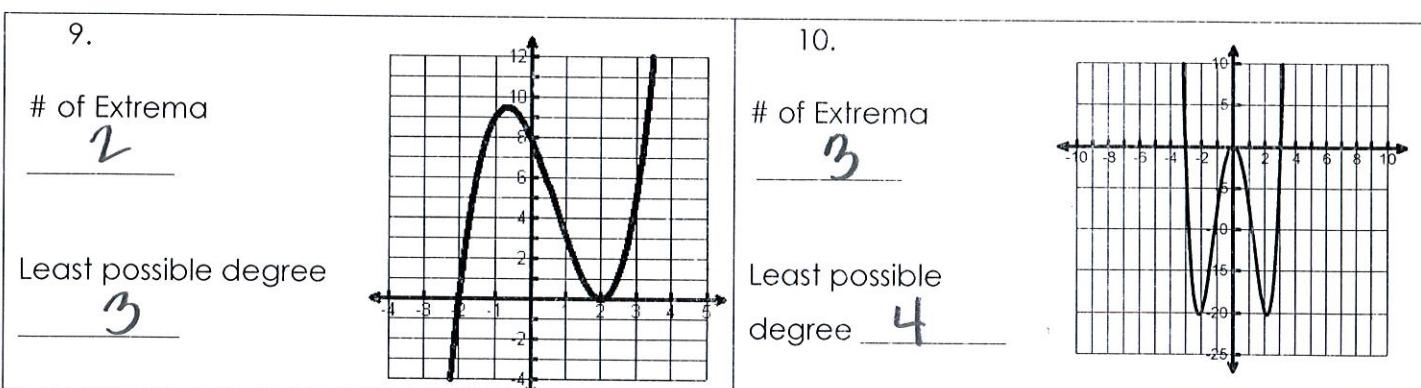
Function	Leading Coeff (+ or -)	Degree	End Behavior
1. $f(x) = x^3 - x^2 - 8x + 12$	+	3 ↗ ↙ 3 ↗	As $x \rightarrow \infty f(x) \rightarrow \infty$ As $x \rightarrow -\infty f(x) \rightarrow -\infty$
2. $f(x) = 3x^3 - 12x + 4$	+	3 ↗ ↙ 3 ↗	As $x \rightarrow \infty f(x) \rightarrow \infty$ As $x \rightarrow -\infty f(x) \rightarrow -\infty$
3. $f(x) = -2x^3 + 4x^2 + x - 2$	-	3 ↗ ↙ 3 ↗	As $x \rightarrow \infty f(x) \rightarrow -\infty$ As $x \rightarrow -\infty f(x) \rightarrow \infty$
4. $f(x) = x^4 + 5x^3 + 5x^2 - x - 6$	+	↑ 4 ↑	As $x \rightarrow \infty f(x) \rightarrow \infty$ As $x \rightarrow -\infty f(x) \rightarrow \infty$
5. $f(x) = -x^4 + 2x^3 - 5x^2 - 6x$	-	↓ 4 ↓	As $x \rightarrow \infty f(x) \rightarrow -\infty$ As $x \rightarrow -\infty f(x) \rightarrow -\infty$

Use the equations to answer the following:

degree - one

Function	Degree	Max # of Extrema
6. $f(x) = x^3 - x^2 - 8x + 12$	3	2
7. $f(x) = -12x^2 + 4$	2	1
8. $f(x) = x^4 + 2x^3 - 5x^2 - 6x$	4	3

Given the graphs, state the Max # of Extrema and the Least Possible Degree



Determine the end behavior and maximum number of extrema (u-turns) w/o calculator:

$$f(x) = -8x^5 - 7x^3 + 3x - 7 \quad \text{Neg & Odd} \quad \downarrow$$

11. $x \rightarrow +\infty f(x) \rightarrow -\infty$ extrema 4
 $x \rightarrow -\infty f(x) \rightarrow \infty$ maxima

$$f(x) = 1 - 3x - 2x^2 - 5x^3 + 7x^4 - 12x^5 \quad \text{Neg & Odd} \quad \downarrow$$

13. $x \rightarrow +\infty f(x) \rightarrow -\infty$ extrema 4
 $x \rightarrow -\infty f(x) \rightarrow +\infty$

$$f(x) = 12 - 3x^3 + 5x^3 - 7x^4 \quad \text{Neg & Even} \quad \downarrow$$

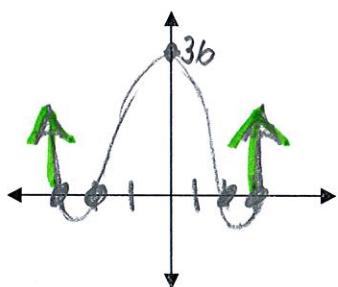
12. $x \rightarrow +\infty f(x) \rightarrow -\infty$ extrema 3
 $x \rightarrow -\infty f(x) \rightarrow -\infty$

$$f(x) = -7x^3 + 343 \quad \text{Neg & Odd} \quad \downarrow$$

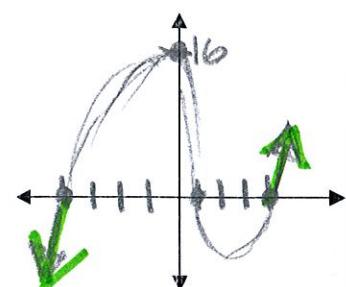
14. $x \rightarrow +\infty f(x) \rightarrow -\infty$ extrema 2
 $x \rightarrow -\infty f(x) \rightarrow \infty$

Find the number of zeros, y-int, & end behavior. Sketch the graph:

15. $x^4 - 13x^2 + 36 = 0 \quad \text{Pos & Even} \uparrow \uparrow$
given zeros: -3, -2, 2, 3



16. $x^3 - x^2 - 16x + 16 = 0 \quad \text{Pos & Odd} \quad \uparrow$
given zeros: -4, 1, 4



of Zeros: 4

Y-Int: (0, 36)

$x \rightarrow +\infty f(x) \rightarrow \infty$

$x \rightarrow -\infty f(x) \rightarrow \infty$

max # of extrema 3

of Zeros: 3

Y-Int: (0, 16)

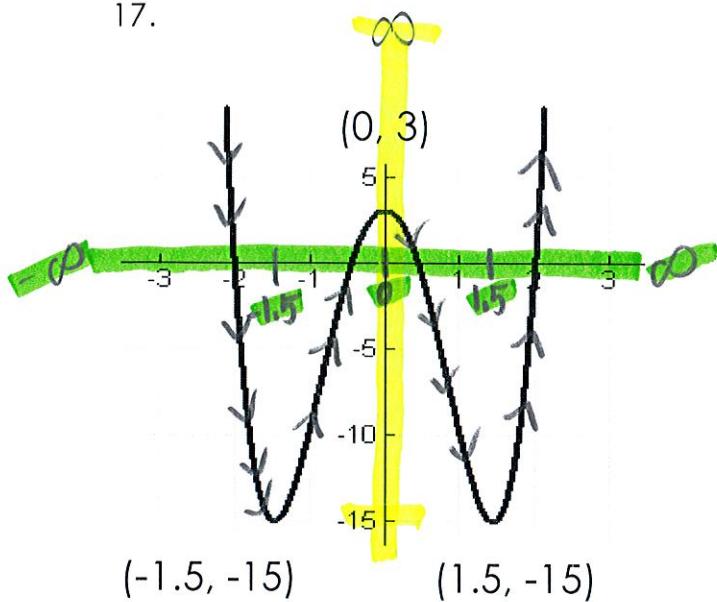
$x \rightarrow +\infty f(x) \rightarrow \infty$

$x \rightarrow -\infty f(x) \rightarrow -\infty$

max # of extrema 2

Answer all of the following questions for the following graph:

17.



Domain: $(-\infty, \infty)$	Range: $(-\infty, \infty)$
Increasing: $(-1.5, 0) (1.5, \infty)$	Decreasing: $(-\infty, -1.5) (0, 1.5)$
x-intercepts: $(-2, 0) (-0.5, 0)$	y-intercept: $(0, 3)$
Abs. Max: $\uparrow \uparrow$ none	Abs. Min: $(-1.5, -15) \& (1.5, 15)$
Rel. Max: $(0, 3)$	Rel. Min: none
Min. degree: 4	Sign of leading Coeff. Positive

turns plus one b.c. $\uparrow \uparrow$